Curriculum Framework Grade 8

| Strand: | Patterns, | Functions, | and Algebra |
|----------------|-----------|------------|-------------|
| | | | |

8.15 The student will

- a) determine whether a given relation is a function; and
- b) determine the domain and range of a function.

Suggested Pacing

First Nine Weeks – 6 Instructional Days (including common assessment)

Related Standards

Spiral Down

7.10 The student will

e) make connections between and among representations of a proportional or additive relationship between two quantities using verbal description, tables, equations, and graphs.

6.12 The student will

d) make connections between and among representations of a proportional relationship between two quantities using verbal descriptions, ratio tables, and graphs.

Spiral Up

- **A.7** The student will investigate and analyze linear and quadratic function families and their characteristics both algebraically and graphically, including
 - a) determining whether a relation is a function;
 - b) domain and range
 - f) connections between and among multiple representations of functions using verbal descriptions, tables, equations, and graphs.

Essential Questions

What is the relationship among tables, graphs, rules and words in modeling a given situation?

Any given relationship can be represented by all four.

What is a relation?

A relation is any set of ordered pairs. For each first member, there may be many second members.

Common Misconceptions

- Students need to practice when given an equation identifying the related graph.
- Students need additional practice determining the domain or range when given an equation and an identified set of values.
- Students need additional practice identifying the dependent variable and independent variable when given a practical problem.

(VDOE – Spring 2014 Student Performance Analysis comment)

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|----------|------|-----|-------|----|
| What | is a | tun | ction | 17 |

A function is a relation between a set of inputs, called the domain, and a set of outputs, called the range, with the property that each input is related to exactly one output.

What is the relationship between relations and functions?

Some relations are functions; all functions are relations.

What is the difference between discrete and continuous functions?

In a discrete function graph there are separate, distinct points. You would not use a line to connect these points on a graph. The points between the plotted points have no meaning and cannot be interpreted. For example, the number of pets per household represents a discrete function because you cannot have a fraction of a pet.

What are terms used to represent the x-value?

Independent variable, input, and domain.

What are terms used to represent the y-value?

Dependent variable, output and range.

| Understanding the Standard | Essential Knowledge and Skills |
|--|---|
| A relation is any set of ordered pairs. For each first member, there may be many second members. | The student will use problem solving, mathematical communication, mathematical reasoning, connections, and representations to |

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- A function is a relation between a set of inputs, called the domain, and a set of outputs, called the range, with the property that each input is related to exactly one output.
- As a table of values, a function has a unique value assigned to the second variable for each value of the first variable. In the "not a function" example, the input value "1" has two different output values, 5 and -3, assigned to it, so the example is not a function.

function

| x | y |
| 2 | 3 |
| 1 | 5 |
| 0 | 3 |
| -1 | -3 |

| x | у |
|---|----|
| 2 | 3 |
| 1 | 5 |
| 0 | 4 |
| 1 | -3 |

- As a set of ordered pairs, a function has a unique or different y-value assigned to each x-value. For example, the set of ordered pairs, {(1, 2), (2, 4), (3, 2), (4, 8)} is a function. This set of ordered pairs, {(1, 2), (2, 4), (3, 2), (2, 3)}, is not a function because the x-value of "2" has two different y-values.
- As a graph of discrete points, a relation is a function when, for any value of x, a vertical line passes through no more than one point on the graph.
- Some relations are functions; all functions are relations.
- Graphs of functions can be discrete or continuous.
- In a discrete function graph there are separate, distinct points. You would not use a line to connect these points on a graph. The points between the plotted points have no meaning and cannot be interpreted. For example, the number of pets per household

- Determine whether a relation, represented by a set of ordered pairs, a table, or a graph of discrete points is a function. Sets are limited to no more than 10 ordered pairs. (a)
- Identify the domain and range of a function represented as a set of ordered pairs, a table, or a graph of discrete points. (b)

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represents a discrete function because you cannot have a fraction of a pet.

- Functions may be represented as ordered pairs, tables, graphs, equations, physical models, or in words. Any given relationship can be represented using multiple representations.
- A discussion about determining whether a continuous graph of a relation is a function using the vertical line test may occur in grade eight, but will be explored further in Algebra I.



- The domain is the set of all the input values for the independent variable or *x*-values (first number in an ordered pair).
- The range is the set of all the output values for the dependent variable or *y*-values (second number in an ordered pair
- If a function is comprised of a discrete set of ordered pairs, then the domain is the set of all the *x*-coordinates, and the range is the set of all the *y*-coordinates. These sets of values can be determined given different representations of the function.
 - Example: The domain of a function is {-1, 1, 2, 3} and the range is {-3, 3, 5}. The following are representations of this function:
 - o The function represented as a table of values:

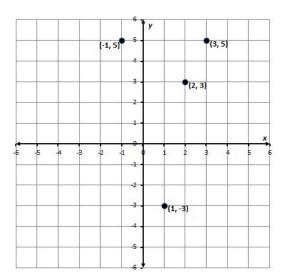
| X | У |
|----|---|
| -1 | 5 |

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o The function represented as a set of ordered pairs:

$$\{(-1, 5), (1, -3), (2, 3), (3, 5)\}$$

o The function represented as a graph on a coordinate plane:



| Vocabulary | Instructional Activities Organized by Learning Objective |
|----------------------|--|
| Relation | Virginia Department of Education |
| Member | |
| Function | Textbook |
| Domain | Virginia Pre-Algebra, ©2012, Glencoe/McGraw-Hill |
| Range | Ordered Pairs and Relations, page(s) 25 – 30 |
| Inputs | • Functions, page(s) 399 – 404 (in part) |
| Outputs | |
| Independent Variable | Notes |
| Dependent Variable | • Relations & Functions |

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| Vertical Line Test Table Ordered Pairs Graph Discrete Continuous X-Value Y-Value Assessment RPS PowerSchool Unit Test – RPS 8.15 Common Assessment Test ID #: | Resources • Print Virginia Coach, NEW SOL Edition, Grade 8, Mathematics Lesson 19 – page 143 (Relations and Functions)(in part) Lesson 20 – page 151 (Describe Functions)(in part) • Technology-based • ExploreLearning.com (Gizmos) – Introduction to Functions – Interactive Instructional Resource(exclude mapping) Station Activities |
| Formative Assessments White Board Checks Kahoot.it Plickers Exit Tickets Graphic Organizers Venn Diagrams | Function/Not A Function Sort - Have students sort cards based on function and not functions. Students should be able to use the vertical line test. Plotting Points on Whiteboards - Have students plot points on whiteboard and determine if a function or not a function. Domain & Range Foldable Function Test Foldable Functions Domain and Range Relations Graphic Organizer(change mapping to ordered pairs) Functions Graphic Organizer(exclude mapping section) |
| Cross-Curricular Connections | Differentiations |
| English Have students explain the difference between domain, range, IV, and DV. History Discuss the causes and effects of a war. Science | Have students make a table when given an equation using the given input values. Have students list ordered pairs when given a function table or after creating a function table. Have students use the ordered pairs to graph the function. Have students match equations, function tables, ordered pairs, and graphs. |

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| Give examples of science fair projects that students have done. | Have |
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| students identify the IV and DV of a given scenario. | |

- Have students determine the independent and dependent variables from a graph and a practical problems.
- Have students highlight independent and dependent variables from a practical problem and connect that to its graph.